

Problem 1: If $\vec{F}(x, y) = \nabla(x^2 + y^4)$, find $\int_C \vec{F} \cdot d\vec{r}$ where C is the quarter of the circle $x^2 + y^2 = 4$ in the first quadrant, oriented counterclockwise.

Problem 2: Compute $\int_C \vec{F} \cdot d\vec{r}$ for each of the following parts.

(a) $\vec{F}(x, y) = [3x^2 \quad 4y^3]^T$ and C is the top of the unit circle from $(1, 0)$ to $(-1, 0)$.

(b) $\vec{F}(x, y) = y \sin(xy)\vec{i} + x \sin(xy)\vec{j}$ and C is the parabola $y = x^2$ from $(1, 1)$ to $(2, 4)$.

(c) $\vec{F}(x, y, z) = [ye^{xy} \quad xe^{xy} \quad \cos(z)]^T$ and C consists of the line from $(0, 0, \pi)$ to $(1, 1, \pi)$ followed by the parabola $z = \pi x^2$ in the plane $y = 1$ to the point $(3, 1, 9\pi)$.